

Mast Arm Fatigue

Current as of March 18, 2008

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Sample:

10-2S-WY-PB-A

Geometry:

Results:

Length: 86 11/16

All lengths measured in inches

Sr	12
Smean	22
Cycles	6,734,487
Location:	

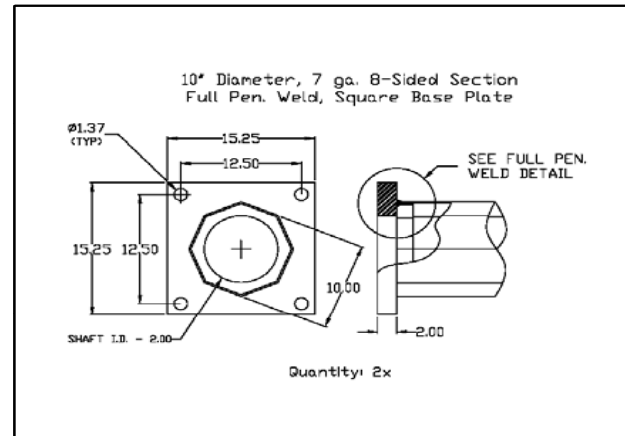
Mast Arm		
	Diameter	Thickness
1	9 3/4	0.192
2	9 13/16	0.194
3	9 15/16	0.190
Average	9.833	0.192

Base Plate		
	Weld	
Thickness	Wall	Baseplate
2.035	9/16	1/4
2.028	5/8	1/4
2.035	9/16	1/4
2.033	0.583	0.250

Loads:

Modulus	13.390	in ³	P _{max}	8.537	kip
S _{max}	28	ksi	P _{min}	4.885	kip
S _{min}	16	ksi			

View from 45° left of vertical



Sample:

10-2S-WY-PB-B

Geometry:

Results:

Length:

All lengths measured in inches

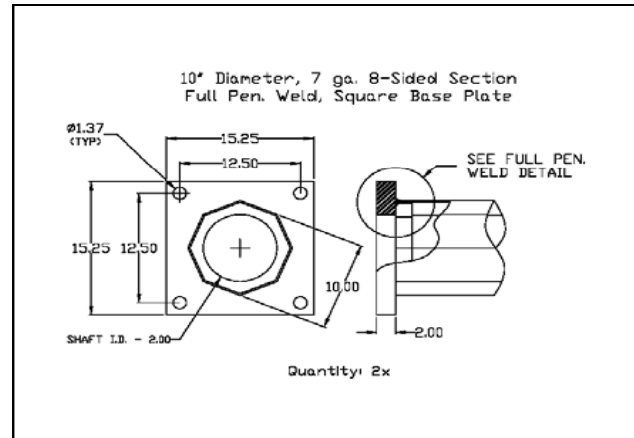
Sr	12
Smean	22
Cycles	5,219,304
Location:	Base Plate Weld Toe

Mast Arm		
	Diameter	Thickness
1	10	0.19
2	9 13/16	0.19
3	10	0.183
Average	9.938	0.188

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.035	9/16	1/4
2.03	5/8	1/4
2.035	5/8	1/4
2.033	0.604	0.250

Loads:

Modulus	<input type="text"/>	in ³	P _{max}	<input type="text"/>	kip
S _{max}	<input type="text"/>	ksi	P _{min}	<input type="text"/>	kip
S _{min}	<input type="text"/>	ksi			



Sample:

10-2S-WY-VG-A

Geometry:

Results:

Length: 86 11/16

All lengths measured in inches

Sr	12
Smean	22
Cycles	12,602,940
Location:	RUNOUT

Mast Arm		
Diameter	Thickness	
1	10	0.195
2	9 15/16	0.183
3		0.19
Average	9.969	0.189

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.016	3/4	2/5
2.012	11/16	3/8
2.014	11/16	11/32
2.014	0.7083	0.375

Loads: (Average section modulus for both sample A and B)

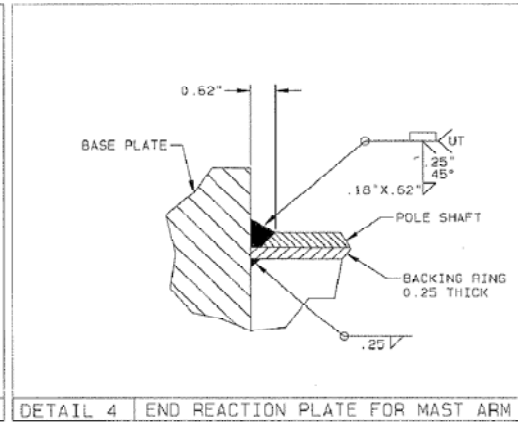
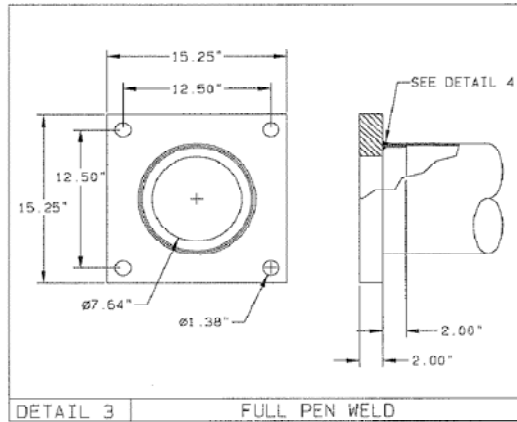
Modulus 13.230 in³

P_{max} 8.335 kip

P_{min} 4.763 kip

S_{max} 28 ksi

S_{min} 16 ksi



Sample:

10-2S-WY-VG-B

Geometry:

Results:

Length: 86 5/8

All lengths measured in inches

Sr	12
S _{mean}	22
Cycles	12,602,940
Location:	RUNOUT

Mast Arm		
	Diameter	Thickness
1	10	0.186
2	10	0.186
3		0.185
Average	10	0.186

Base Plate		
	Weld	
Thickness	Wall	Baseplate
2.014	5/8	1/3
2.016	13/16	7/16
2.031	3/4	7/16
2.02	0.729	0.396

Loads: (Average section modulus for both sample A and B)

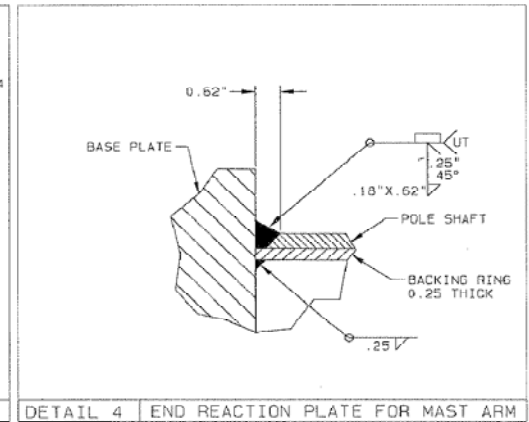
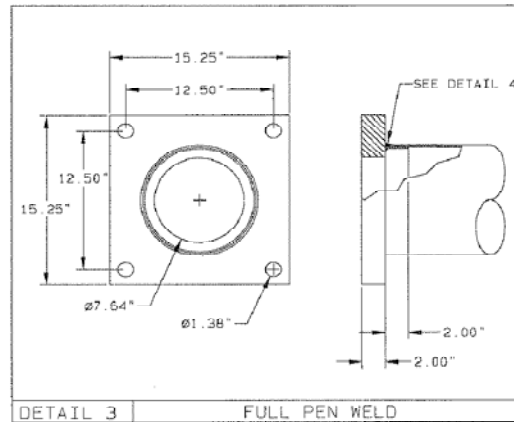
Modulus 13.230 in³

P_{max} 8.335 kip

P_{min} 4.763 kip

S_{max} 28 ksi

S_{min} 16 ksi



Sample:

8-2S-WY-VG-A

Geometry:

Length: 86 5/8

All lengths measured in inches

Results:

Failure 1

Sr	24
Smean	22
Cycles	856,122
Location:	Backing bar

Failure 2

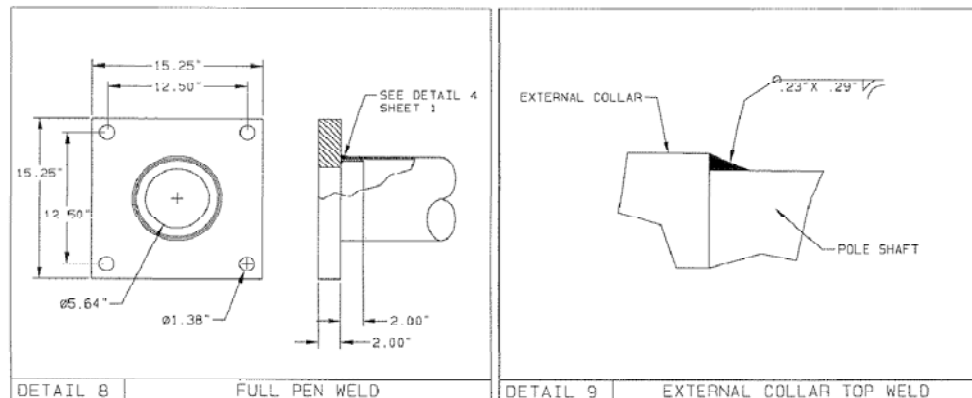
Sr	24
Smean	22
Cycles	747,510
Location:	Weld toe

Mast Arm		
	Diameter	Thickness
1	8	0.17
2	7 15/16	0.168
3		0.17
Average	7.969	0.169

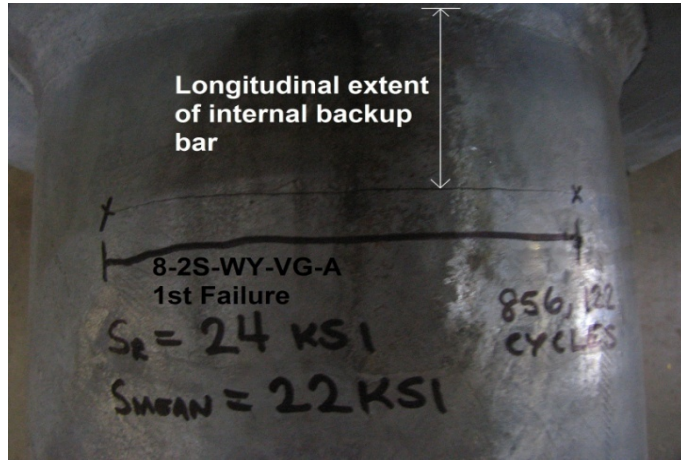
Base Plate		
	Weld	
Thickness	Wall	Baseplate
2.016	7/16	13/16
2.017	7/16	7/8
2.008	7/16	13/16
2.014	7/16	0.833

Loads: (average modulus for A and B)

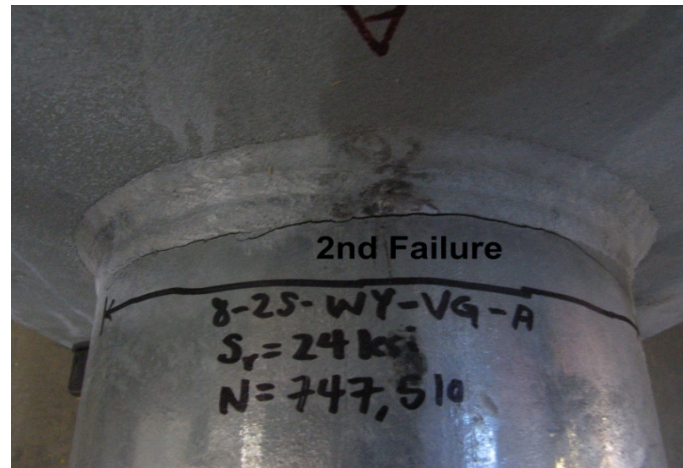
Modulus	7.862 in ³	P _{max}	6.017 kip
		P _{min}	1.77 kip
S _{max}	34 ksi		
S _{min}	10 ksi		



Failure 1



Failure 2



Back up bar fit up



Sample:

8-2S-WY-VG-B

Geometry:

Results:

Length: 86 5/8

All lengths measured in inches

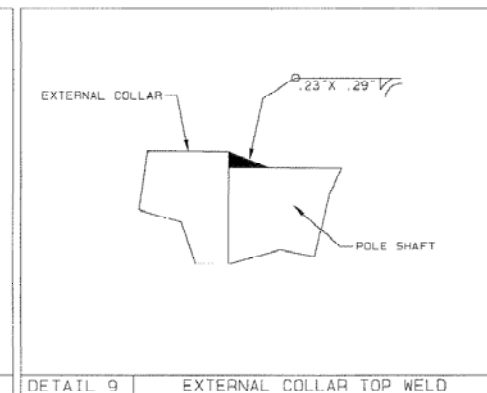
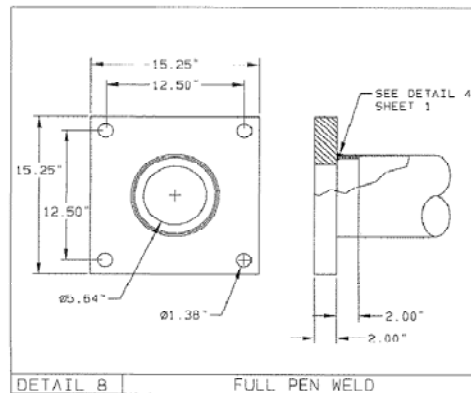
Sr	24
Smean	22
Cycles	1,603,632
Location:	RUNOUT

Mast Arm		
Diameter	Thickness	
1	8	0.163
2	7 15/16	0.166
3		0.168
Average	7.98	0.166

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.017	7/16	13/16
	7/16	7/8
	7/16	7/8
2.017	7/16	0.854

Loads: (average modulus for A and B)

Modulus	7.862	in ³	P _{max}	6.017	kip
S _{max}	34	ksi	P _{min}	1.77	kip
S _{min}	10	ksi			



Sample:

8-2S-EC-VG-A

Geometry:

Results:

Length: 86 5/8

All lengths measured in inches

Sr	18
S _{mean}	22
Cycles	512,860
Location:	COLLAR WELD

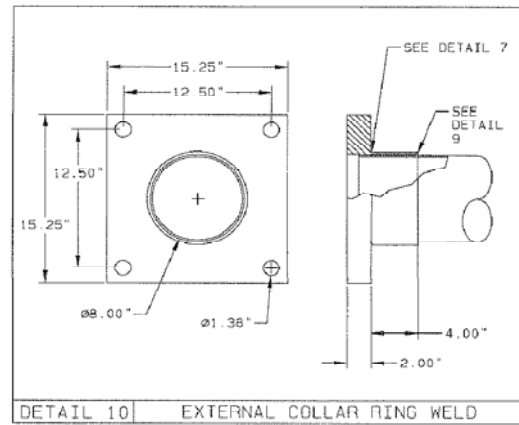
Mast Arm		
	Diameter	Thickness
1	7 9/16	0.186
2	7 9/16	0.19
3		0.194
Average	7 9/16	0.19

Base Plate		
	Weld	
Thickness	Wall	Baseplate
1.997	13/16	13/32
1.996	13/16	7/16
2.044	13/16	13/32
2.0123	0.813	0.417

Loads: (average for A and B)

Modulus	8.712 in ³	P _{max}	6.077 kip
S _{max}	31 ksi	P _{min}	2.549 kip
S _{min}	13 ksi		

Collar		
	Weld	
Height	Wall	Collar
4 1/16	5/8	1/4
4 1/8	9/16	1/4
	5/8	1/4
4 3/32	0.604	0.25



Sample:

8-2S-EC-VG-B

Geometry:

Results:

Length: 86 11/16

All lengths measured in inches

Sr	18
Smean	22
Cycles	653,208
Location:	COLLAR WELD

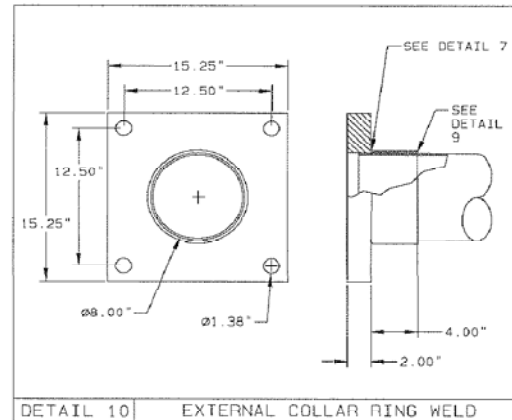
Mast Arm		
	Diameter	Thickness
1	7 5/8	0.186
2	7 5/8	0.188
3		0.181
Average	7 5/8	0.185

Base Plate		
	Weld	
Thickness	Wall	Baseplate
1.992	3/4	1/3
1.991	11/16	3/8
1.990	3/4	5/16
1.991	0.729	0.333

Loads: (average for A and B)

Modulus	8.712 in ³	P _{max}	6.077 kip
S _{max}	31 ksi	P _{min}	2.549 kip
S _{min}	13 ksi		

Collar		
	Weld	
Height	Wall	Collar
4	9/16	1/5
4	5/8	5/16
	9/16	3/16
4	0.583	0.229



Sample:

12-2S-WY-VG-A

Geometry:

Results:

Length: 86 5/8

All lengths measured in inches

Sr	18
S _{mean}	22
Cycles	1,053,554
Location:	Base plate weld toe

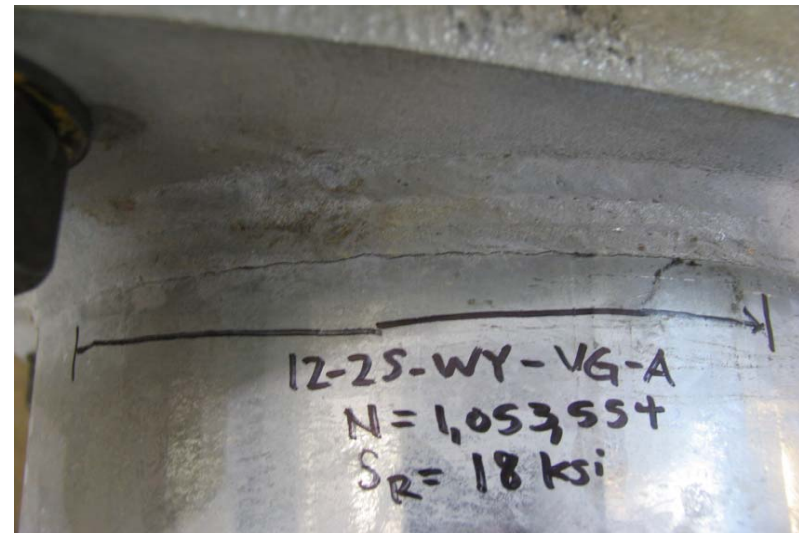
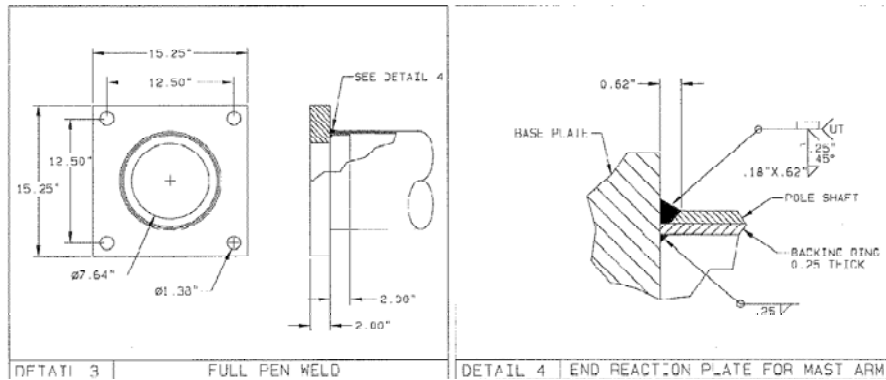
Mast Arm		
	Diameter	Thickness
1	7 9/16	0.186
2	7 9/16	0.19
3		0.194
Average	7 9/16	0.19

Base Plate		
	Weld	
Thickness	Wall	Baseplate
1.997	5/8	1/4
1.996	9/16	1/4
2.044	5/8	1/4
2.012	0.604	0.250

Loads:

Modulus 18.980 in³ P_{max} 5.540 kip
 P_{min} 13.22 kip

S_{max} 31 ksi
 S_{min} 13 ksi



Sample:

12-2S-WY-VG-B

Geometry:

Results:

Length: 85 15/16

All lengths measured in inches

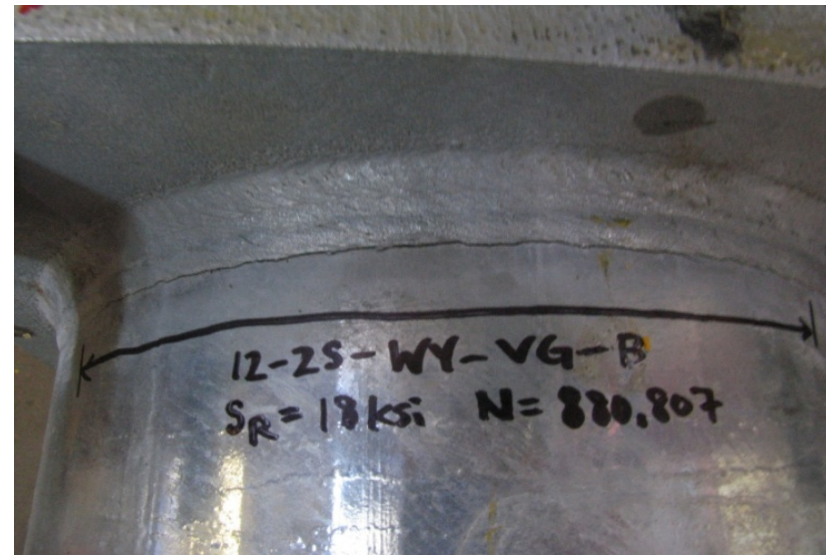
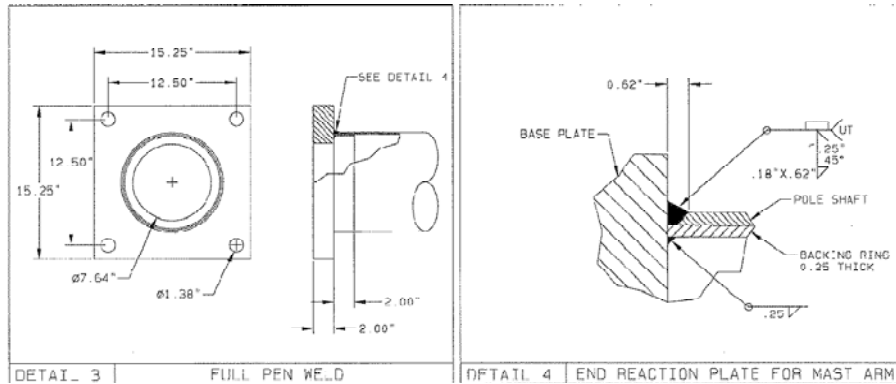
Sr	18
Smean	22
Cycles	880,807
Location:	Base Plate Weld

Mast Arm		
Diameter	Thickness	
1	12	0.178
2	11 13/16	0.179
3		0.177
Average	11.969	0.178

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.055	13/16	1/2
1.989	13/16	7/16
2.010	13/16	7/16
2.018	0.8125	0.458

Loads:

Modulus 19.050 in^3 $P_{\max} 13.270 \text{ kip}$
 $P_{\min} 5.565 \text{ kip}$
 $S_{\max} 31 \text{ ksi}$
 $S_{\min} 13 \text{ ksi}$



Sample:

12-2S-EC-VG-A

Geometry:

Results:

Length: 85 15/16

All lengths measured in inches

Sr	18
Smean	22
Cycles	805,991
Location:	RUNOUT

Mast Arm		
	Diameter	Thickness
1	11 5/8	0.178
2	11 1/16	0.179
3		0.18
Average	11.344	0.179

Base Plate		
	Weld	
Thickness	Wall	Baseplate
2.003	11/16	5/16
1.999	11/16	5/16
2.008	5/8	9/32
2.003	0.667	0.302

Loads: (average for A and B)

Modulus 19.174 in³

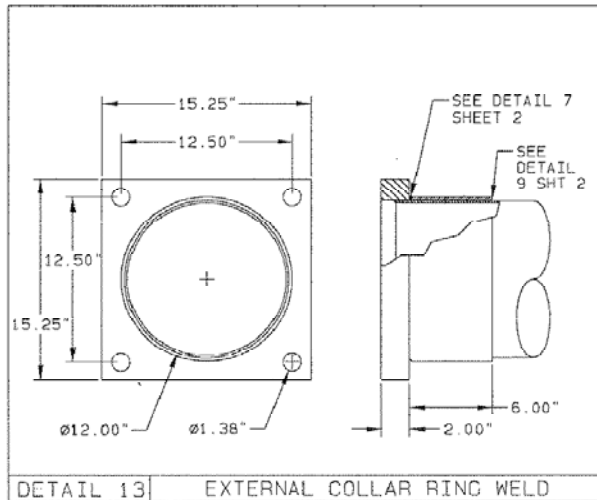
P_{max} 13.375 kip

P_{min} 5.609 kip

S_{max} 31 ksi

S_{min} 13 ksi

Collar		
	Weld	
Height	Wall	Collar
6	5/8	1/4
6	5/8	1/4
	5/8	1/4
6	0.625	0.250



Sample:

12-2S-EC-VG-B

Geometry:

Length: 85 7/8

All lengths measured in inches

Results:

Failure 1

Sr	18
Smean	22
Cycles	468,601
Location:	Collar Weld Toe

Failure 2

Sr	18
Smean	22
Cycles	337,390
Location:	Collar Weld Toe

Mast Arm	
Diameter	Thickness
1 11 5/8	0.178
2 11 11/16	0.179
3	0.239
Average	11.656
	0.199

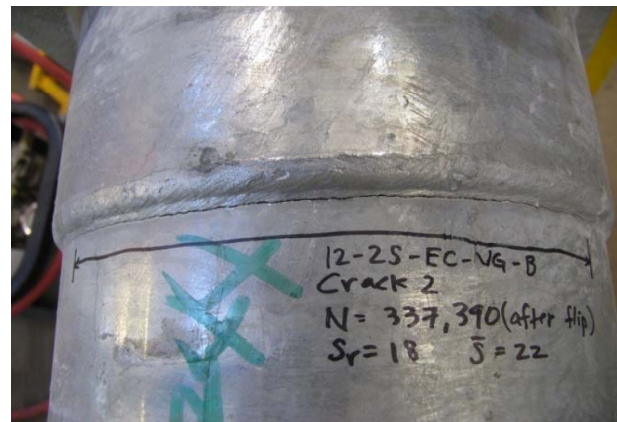
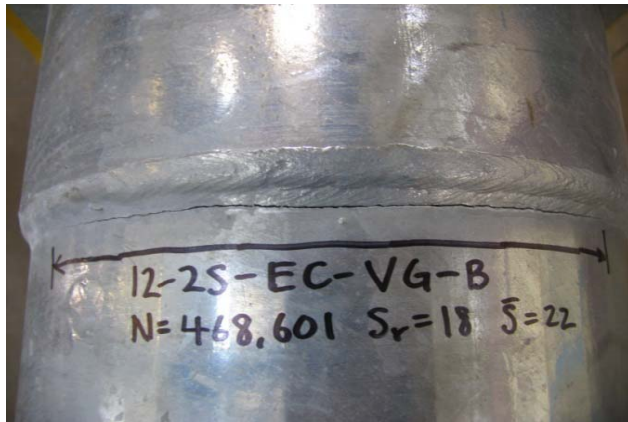
Base Plate		
Weld		
Thickness	Wall	Baseplate
1.996	3/4	7/16
1.994	3/4	1/2
2.010	7/8	15/32
2.000	0.792	0.469

Collar		
Weld		
Height	Wall	Collar
6 1/8	5/8	1/4
6 1/8	1/2	9/32
	9/16	1/4
6 1/8	0.563	0.260

Loads: (average modulus for A and B)

Modulus 19.174 in³ P_{max} 13.375 kip
P_{min} 5.609 kip

S_{max} 31 ksi
S_{min} 13 ksi



Sample:

10-3R-WY-VG-A

Geometry:

TEST 1

Results:

Length: 86 11/16

All lengths measured in inches

Sr	18
Smean	22
Cycles	8,037,420
Location:	RUNOUT

Mast Arm	
Diameter	Thickness
1	9 15/16 0.177
2	9 15/16 0.175
3	0.174
Average	9 15/16 0.175

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.025	23/32	9/32
3.024	3/4	11/32
3.027	25/32	3/8
3.025	0.750	0.333

Loads:

Modulus 12.801 in³

P_{max} 9.032 kip

P_{min} 3.788 kip

S_{max} 31 ksi

S_{min} 13 ksi

Sample:

10-3R-WY-VG-B

TEST 1

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Sr	18
Smean	22
Cycles	8,037,420
Location:	RUNOUT

Mast Arm	
Diameter	Thickness
1 9 15/16	0.176
2 9 7/8	0.17
3	0.175
Average	9 29/32
	0.174

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.021	3/4	9/32
3.019	3/4	11/32
3.025	23/32	9/32
3.022	0.740	0.302

Loads:

Modulus 12.801 in³

P_{max} 9.032 kip

P_{min} 3.788 kip

S_{max} 31 ksi

S_{min} 13 ksi

Sample:

10-3R-WY-VG-A

Geometry:

TEST 2

Results:

Length: 86 3/4

All lengths measured in inches

Sr	24
Smean	22
Cycles	439,511
Location:	

Mast Arm	
Diameter	Thickness
1 9 15/16	0.177
2 9 15/16	0.175
3	0.174
Average	9 15/16 0.175

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.025	23/32	9/32
3.024	3/4	11/32
3.027	25/32	3/8
3.025	0.750	0.333

Loads:

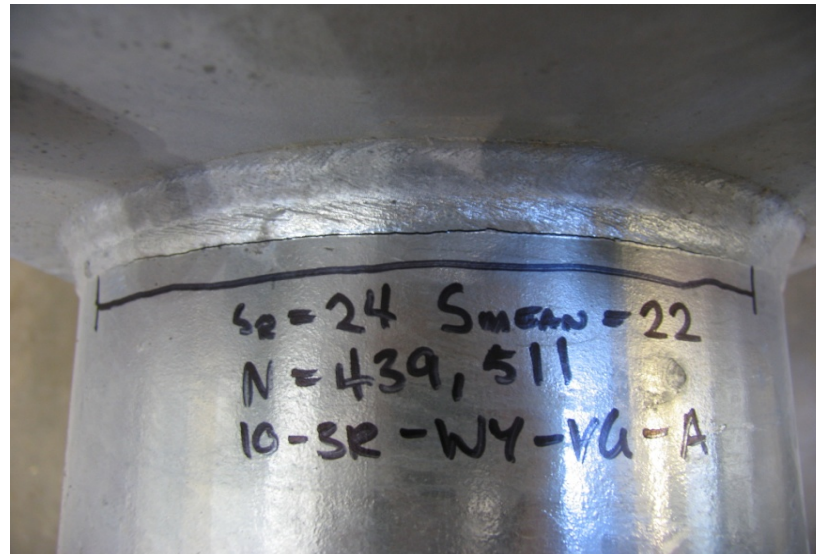
Modulus 12.801 in³

P_{max} 9.906 kip

P_{min} 2.914 kip

S_{max} 34 ksi

S_{min} 10 ksi



Sample:

10-3R-WY-VG-B

Geometry:

TEST 2

Results:

Length: 86 3/4

All lengths measured in inches

Sr	24
Smean	22
Cycles	343,175
Location:	Weld Toe

Mast Arm		
	Diameter	Thickness
1	9 15/16	0.176
2	9 7/8	0.17
3		0.175
Average	9 29/32	0.174

Base Plate		
	Weld	
Thickness	Wall	Baseplate
3.021	3/4	9/32
3.019	3/4	11/32
3.025	23/32	9/32
3.022	0.740	0.302

Loads:

Modulus 12.801 in³

P_{max} 9.906 kip

P_{min} 2.914 kip

S_{max} 34 ksi

S_{min} 10 ksi



Effective Stress Range Calculations

10-3R-WY-VG-A

Sr1 =	18
Sr2 =	24
n18 =	8037420
n24 =	343175
Ntot =	8380595
γ_{18} =	0.959051
γ_{24} =	0.040949
(Sr)eff =	18.33

10-3R-WY-VG-B

Sr1 =	18
Sr2 =	24
n18 =	8037420
n24 =	439511
Ntot =	8476931
γ_{18} =	0.948152
γ_{24} =	0.051848
(Sr)eff =	18.42

Miners Rule:

$$S_{r,eff} = \left(\sum \gamma_i S_r^3 \right)^{1/3}$$

Sample:

10-3R-WY-VG-A
Effective Stress Range

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Sr	18.33
Smean	
Cycles	8,380,595
Location:	

Mast Arm	
Diameter	Thickness
1 9 15/16	0.177
2 9 15/16	0.175
3	0.174
Average	9 15/16 0.175

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.025	23/32	9/32
3.024	3/4	11/32
3.027	25/32	3/8
3.025	0.750	0.333

Loads:

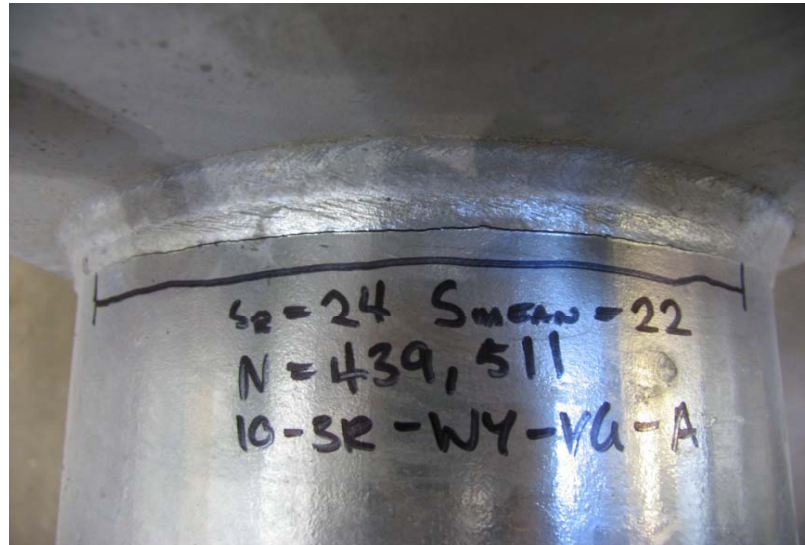
Modulus 12.801 in³

P_{max} 9.906 kip

P_{min} 2.914 kip

S_{max} 34 ksi

S_{min} 10 ksi



Sample:

10-3R-WY-VG-B
Effective Stress Range

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Sr	18.42
Smean	
Cycles	8,476,931
Location:	Weld Toe

Mast Arm	
Diameter	Thickness
1 9 15/16	0.176
2 9 7/8	0.17
3	0.175
Average	9 29/32
	0.174

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.021	3/4	9/32
3.019	3/4	11/32
3.025	23/32	9/32
3.022	0.740	0.302

Loads:

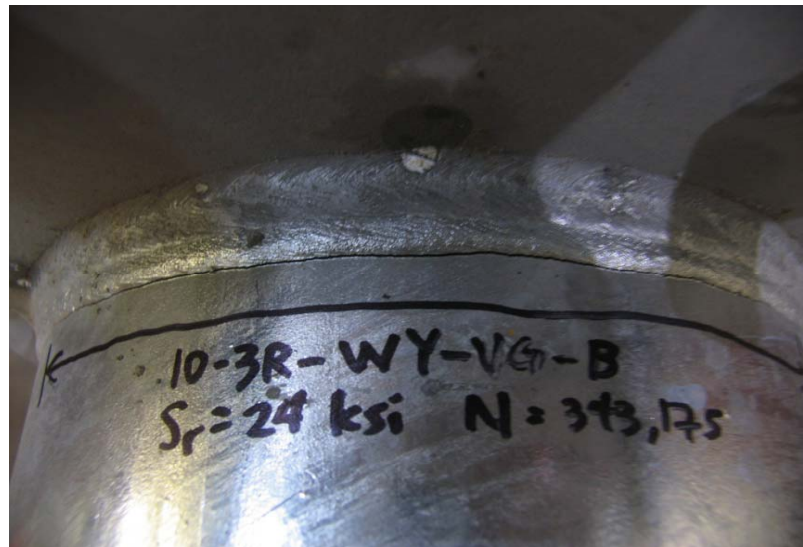
Modulus 12.801 in³

P_{max} 9.906 kip

P_{min} 2.914 kip

S_{max} 34 ksi

S_{min} 10 ksi



Sample:

10-3R-WY-VP-A

Geometry:

Results:

Length: 86 11/16

All lengths measured in inches

Sr	24
Smean	22
Cycles	10,055,123
Location:	RUNOUT

Mast Arm	
Diameter	Thickness
1	9 15/16 0.177
2	9 15/16 0.178
3	0.177
Average	9 15/16 0.177

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.025	25/32	2/7
3.014	25/32	9/32
3.025	13/16	5/16
3.021	19/24	7/24

Loads:

Modulus 13.040 in³

P_{max} 10.120 kip

P_{min} 2.98 kip

S_{max} 34 ksi

S_{min} 10 ksi

Sample:

10-3R-WY-VP-B

Geometry:

Results:

Length: 86 11/16

All lengths measured in inches

Sr	24
Smean	22
Cycles	10,055,123
Location:	RUNOUT

Mast Arm	
Diameter	Thickness
1 10	0.177
2 9 15/16	0.178
3	0.176
Average	9 31/32
	0.177

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.007	23/32	5/16
3.007	3/4	11/32
3.016	25/32	3/8
3.010	3/4	11/32

Loads:

Modulus 13.120 in³

P_{max} 10.12 kip

P_{min} 2.98 kip

S_{max} 34 ksi

S_{min} 10 ksi

Sample:

10-3R-WY-VB-A

Geometry:

Incorrect Loads

Results:

Length: 86 3/4

All lengths measured in inches

Sr	16.37
Smean	14.975
Cycles	1,630,350
Location:	RUNOUT

Mast Arm		
	Diameter	Thickness
1	9 15/16	0.182
2	9 15/16	0.179
3		0.176
Average	9 15/16	0.179

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.994	25/32	3/8
2.990	27/32	3/8
2.992		
2.992	13/16	3/8

Loads:

Modulus 13.130 in³

P_{max} 6.92 kip

P_{min} 2.03 kip

S_{max} 6.79 ksi

S_{min} 23.16 ksi

Sample:

10-3R-WY-VB-B

Geometry:

Incorrect Loads

Results:

Length: 86 3/4

All lengths measured in inches

Sr	16.37
Smean	14.975
Cycles	1,630,350
Location:	RUNOUT

Mast Arm	
Diameter	Thickness
1	10
2	10
3	
Average	10

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.992	13/16	9/32
2.997	11/16	11/32
2.990		
2.993	3/4	5/16

Loads:

Modulus 13.130 in³

P_{max} 6.92 kip

P_{min} 2.03 kip

S_{max} 23.16 ksi

S_{min} 6.79 ksi

Sample:

10-3R-WY-VB-A

Geometry:

Correct Loads

Results:

Length: 86 3/4

All lengths measured in inches

Failure 1

Sr	24
Smean	22
Cycles	602,392
Location:	Weld Toe

Failure 2

Sr	24
Smean	22
Cycles	490,121
Location:	Weld Toe

Mast Arm		
	Diameter	Thickness
1	9 15/16	0.182
2	9 15/16	0.179
3		0.176
Average	9 15/16	0.179

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.994	25/32	3/8
2.990	27/32	3/8
2.992		
2.992	13/16	3/8

Loads:

Modulus	13.130 in ³	P _{max}	10.16 kip
S _{max}	34 ksi	P _{min}	2.99 kip
S _{min}	10 ksi		

Failure 1



Failure 2



Sample:

10-3R-WY-VB-B

Geometry:

Correct Loads

Results:

Length: 86 3/4

All lengths measured in inches

Sr	24
Smean	22
Cycles	1,886,425
Location:	8" Away from Weld

Mast Arm		
	Diameter	Thickness
1	10	0.175
2	10	0.176
3		0.178
Average	10	0.176

Base Plate		
	Weld	
Thickness	Wall	Baseplate
2.992	13/16	9/32
2.997	11/16	11/32
2.990		
2.993	3/4	5/16

Loads:

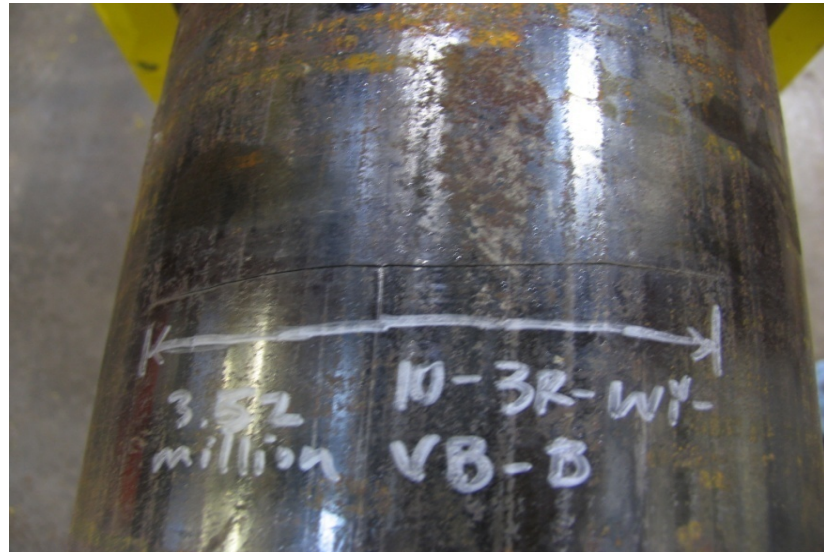
Modulus 13.130 in³

P_{max} 10.16 kip

P_{min} 2.99 kip

S_{max} 34 ksi

S_{min} 10 ksi



Effective Stress Range Calculations

10-3R-WY-VB-A1

Sr1 =	16.37
Sr2 =	24
n18 =	1630350
n24 =	602392
Ntot =	2232742
γ_{18} =	0.730201
γ_{24} =	0.269799
(Sr)eff =	19.07

10-3R-WY-VB-A2

Sr1 =	16.37
Sr2 =	24
n18 =	1630350
n24 =	1092513
Ntot =	2722863
γ_{18} =	0.598763
γ_{24} =	0.401237
(Sr)eff =	20.14

10-3R-WY-VB-B

Sr1 =	16.37
Sr2 =	24
n18 =	1630350
n24 =	1886425
Ntot =	3516775
γ_{18} =	0.463592
γ_{24} =	0.536408
(Sr)eff =	21.14

Miners Rule:

$$S_{r,eff} = \left(\sum \gamma_i S_r^3 \right)^{1/3}$$

Sample:

10-3R-WY-VB-A

Effective

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Failure 1

Sr	19.07
Smean	
Cycles	2,232,742
Location:	Weld Toe

Failure 2

Sr	20.14
Smean	
Cycles	2,722,863
Location:	Weld Toe

Mast Arm	
Diameter	Thickness
1 9 15/16	0.182
2 9 15/16	0.179
3	0.176
Average	9 15/16
	0.179

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.994	25/32	3/8
2.990	27/32	3/8
2.992		
2.992	13/16	3/8

Loads:

Modulus 13.130 in³ P_{max} 10.16 kip

P_{min} 2.99 kip

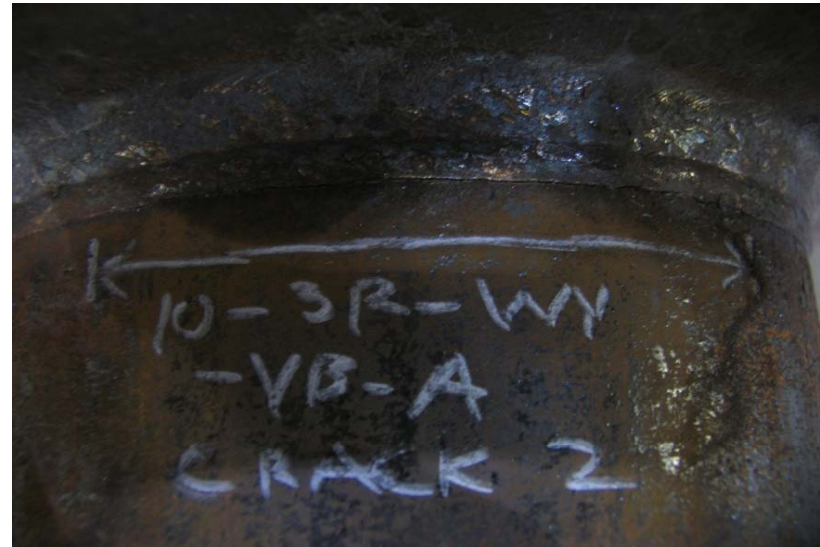
S_{max} 34 ksi

S_{min} 10 ksi

Failure 1



Failure 2



Sample:

10-3R-WY-VB-B

Effective

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Sr	21.14
Smean	
Cycles	3,516,775
Location:	8" Away from Weld

Mast Arm	
Diameter	Thickness
1 10	0.175
2 10	0.176
3	0.178
Average	10 0.176

Base Plate		
Weld		
Thickness	Wall	Baseplate
2.992	13/16	9/32
2.997	11/16	11/32
2.990		
2.993	3/4	5/16

Loads:

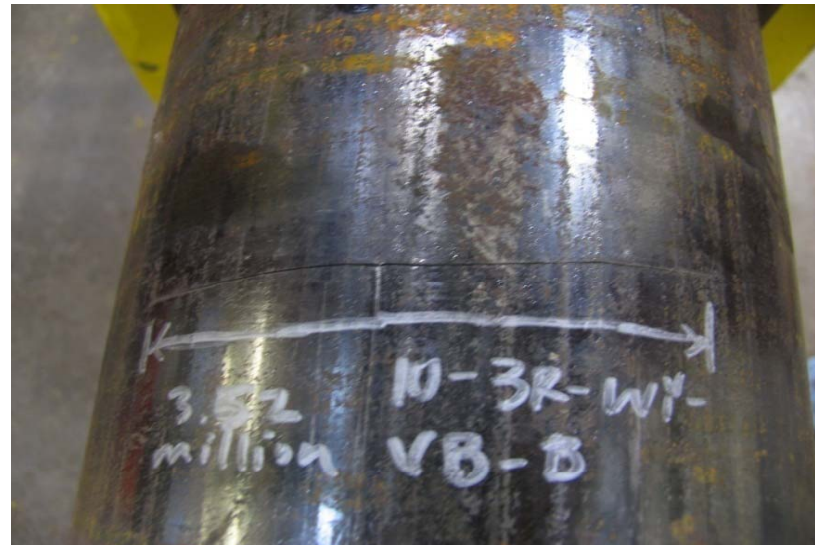
Modulus 13.130 in³

P_{max} 10.16 kip

P_{min} 2.99 kip

S_{max} 34 ksi

S_{min} 10 ksi



Sample:

Ameron A

Geometry:

Length: 86 3/4

All lengths measured in inches

Results:

Failure 1

Sr	24
Smean	22
Cycles	222,649
Location:	

Failure 2

Sr	24
Smean	22
Cycles	212,891
Location:	Weld Toe

Mast Arm	
Diameter	Thickness
1	10
2	10
3	
Average	10
	0.179

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.030	11/16	1/4
3.030	5/8	9/32
3.050		
3.037	21/32	17/64

Loads:

Modulus 13.260 in³

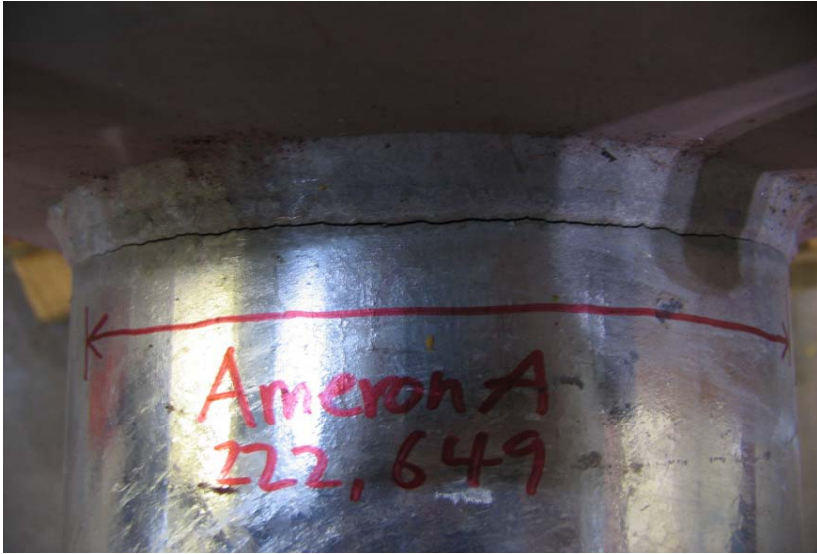
P_{max} 10.29 kip

P_{min} 3.03 kip

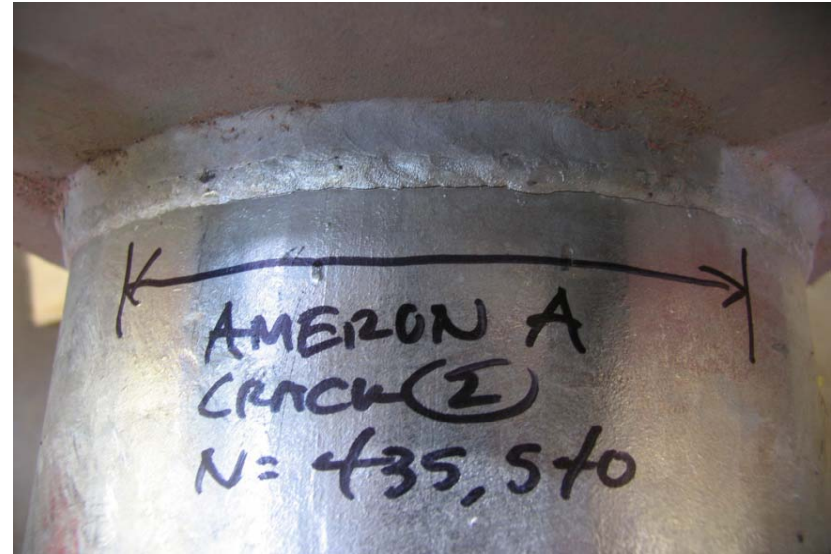
S_{max} 34 ksi

S_{min} 10 ksi

Failure 1



Failure 2



Sample:

Union Metal A

Geometry:

Length: 86 7/8

All lengths measured in inches

Results:

Sr	24
Smean	22
Cycles	1,873,499
Location:	

Mast Arm	
Diameter	Thickness
1 9 15/16	Nominal
2 10	
3	
Average 9 31/32	0.179

Base Plate		
Weld		
Thickness	Wall	Baseplate
3.050	15/32	5/16
3.055	17/32	5/16
3.040		
3.048	1/2	5/16

Loads:

Modulus 13.240 in³

P _{max}	10.29	kip
P _{min}	3.03	kip

S _{max}	34	ksi
S _{min}	10	ksi

